

## **Design of Veneer Cover Soils on Landfills**

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### **Introduction**

**K**oerner and Soong (1998) have presented the slope stability analysis for different scenarios of cover soil in a landfill. They obtained the factor of safety (FS) as a result of the analyses and then they discussed its acceptability for different scenarios.

The geomembrane liner acts as the primary leachate barrier but is susceptible to mechanical damage during construction and subsequent waste placement and must be protected. In order to protect the geomembrane a soil layer is placed which also acts as a drainage layer for leachate.

The sliding of cover soils on slopes underlain by geosynthetics is obviously an unacceptable situation and will eventually reflect on the entire technology. Steeply sloped leachate collection layers are the situations where such slides can occur. The following are the reasons, which pose a major challenge;

- The barrier materials have a low interface shear strength with respect to the soil placed upon them.
- The liner possesses a potential sliding.
- The shear planes are linear.
- Liquid (water or leachate) cannot percolate downward due to the barrier material.

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Here the geotechnical engineering consideration is presented leading to the goal of establishing a suitable factor of safety against the cover soil slope instability. A number of common situations are analyzed which have the tendency to decrease stability, and two numbers of design options are analyzed which increases or enhances the stability. For all the analysis the design charts are presented for typical soil characteristics.

## Cover Soil on Geomembrane Lined Slopes

Cover soil is placed above the geomembrane in landfills to protect the geomembrane liner from the Municipal Solid Waste (MSW) that will be dumped. Cover soil on the geomembrane along with landfill caps and closures are shown in Fig.1. The stability of the overlying materials as well as tensile stresses of the geomembrane should be performed. Single or double liners are used beneath solid and liquid waste. In this analysis, a single geomembrane has been discussed here for the development of design model.

Interface friction considerations:

$$E_c = \left( \frac{C_a}{C} \right) * 100$$

$$E_\phi = \left( \frac{\tan \delta}{\tan \phi} \right) * 100$$

where  $E_c$  = efficiency on cohesion  
 $c$  = cohesion of soil-to-soil  
 $\delta$  = friction angle of soil-to-geomembrane  
 $C_a$  = adhesion of soil-to-geomembrane

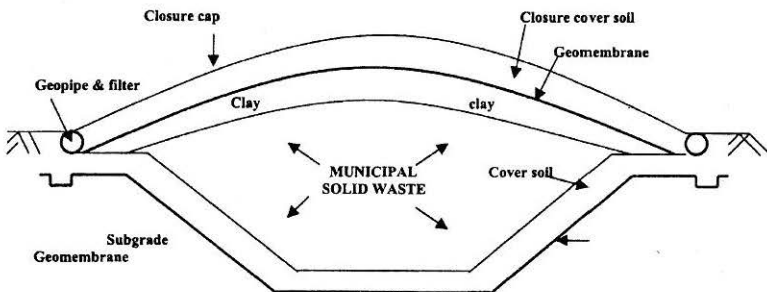


FIGURE 1 : Schematic Diagram of a Landfill showing Major Parts

$E_\phi$  = efficiency of friction

$\phi$  = internal friction angle of the soil

## Stability of Cover Soil having Uniform Thickness

Geomembranes are to be covered with cover soil for the following reasons:

- Protection against oxidation, ultraviolet degradation, accidental damages intentional damage, ice puncture and tearing by sharp objects.
- Eliminating of wind uplift stresses.
- Minimization of temperature.

The covering is a thin layer of soil, which has the tendency when placed on side slopes to slide gravitationally downwards. The frictional resistance between soil and geomembrane is lower than the sub-grade soil. Fig.2 shows the subsoil, geomembrane and cover soil having uniform thickness and the limit equilibrium forces in an infinite slope. The potential failure surface for cover soil is usually linear with the cover soil sliding with respect to the lower interface friction layer in the underlying cross section. The potential failure plane being planer allows for a straightforward stability calculation without the need for trial center locations and different radii as with soil stability problems analyzed by rotational failure surfaces. Furthermore, full static equilibrium can be verified without any assumptions.

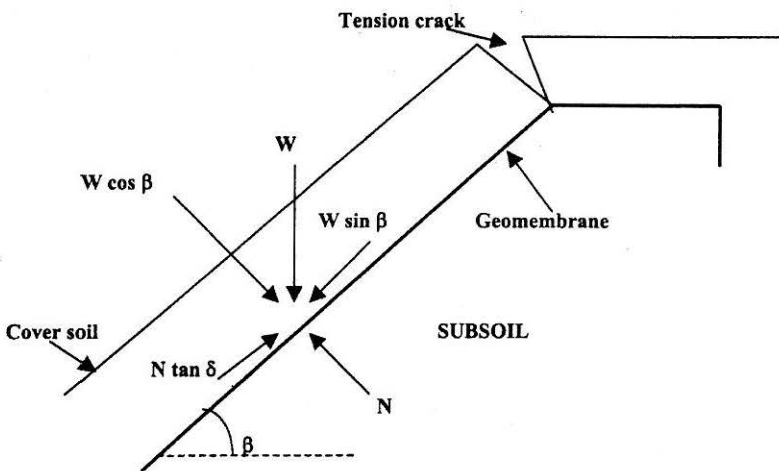


FIGURE 2 : Limit Equilibrium Forces involved in an Infinite Slope Analysis for a Uniformly Thick Cohesionless Cover Soil

Taking force summation parallel to the slope and comparing the resisting force to the driving or mobilizing force treats this situation quite simply. Thus, a factor of safety is determined.

$$\begin{aligned} FS &= \frac{\sum \text{Resisting Forces}}{\sum \text{Driving Forces}} \\ &= N \tan \delta / W \sin \beta \\ &= W \cos \beta \tan \delta / W \sin \beta \\ FS &= \tan \delta / \tan \beta \end{aligned}$$

where,

$W$  = weight of the cover soil

$N$  = reaction normal to the geomembrane =  $W \cos \beta$

$\delta$  = interface friction angle between geomembrane and cover soil

$b$  = Side slope angle with respect to horizontal.

The interface shear strength of a cover soil with respect to the underlying material is critical to properly analyze the stability of the cover soil. This interface shear strength is obtained by laboratory testing. The values of peak shear strength  $\tau_p$  for corresponding normal stress  $\sigma_n$  is plotted to obtain interface friction angle  $\delta$  and cohesion intercept  $c_a$ . In case of design

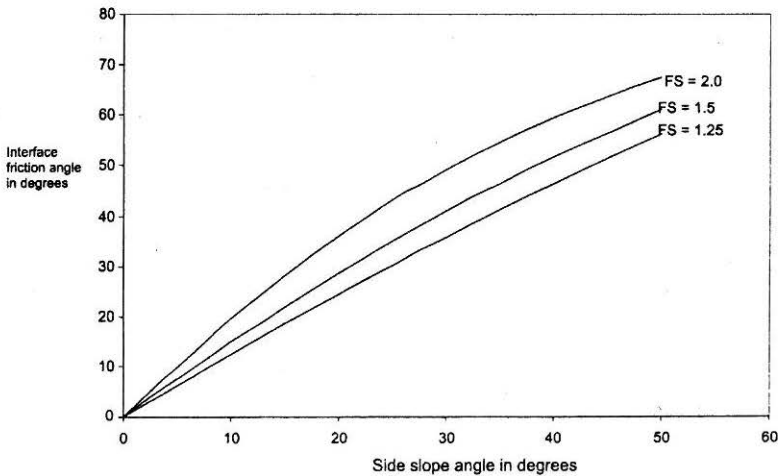


FIGURE 3 : Design Chart, Factor of Safety

we know the slope angle  $\beta$ . A factor of safety is selected (i.e. FS = 1.25, 1.5 or 2). The frictional angle between geomembrane and cover soil is obtained using the above equation or the design chart shown in Fig.3.

Unstable situation may arise due to seepage forces on the cover soil. In addition seismic forces will further reduce the factor of safety. All such situations that cause instability are discussed in detail later. The soil covers on geomembrane-lined slopes are protected against scour by stone riprap, precast concrete blocks, erosion control geosynthetics, or other armoring system. The geomembrane-lined slope with cover soil may fail due to sliding failure of the soil or tension failure of the soil or tension failure of the geomembrane.

### **Situations causing Destabilization of Slopes**

The following are the common situations, which cause destabilizing forces for the slope stability.

- Gravitational forces of the cover soil
- Gravitational forces of the cover soil and construction equipment on the slope
- Gravitational forces of the cover soil and seepage forces
- Gravitational forces of the cover soil and seismic forces

#### ***Gravitational Forces of the Cover Soil***

A finite length slope with uniformly thick cover soil placed over a liner material at a slope angle ' $\beta$ ' is shown in Fig.4. The analysis that follows is after Koerner and Hwu (1991).

The cover soil of unit weight  $\gamma$  and thickness  $h$  is placed on the geomembrane, which is at an angle of  $\beta$  with the horizontal. The shear strength parameters,  $\phi$  and  $c$  and adhesion  $C_a$  and interface friction angle  $\delta$  should be determined in the laboratory. The discrete zones of active and passive wedges are shown in Fig.4. A tension crack may appear at the top of the slope. For the slope stability analysis the factor of safety is obtained as follows:

$$W_A = \gamma h^2 \left( \frac{L}{h} - \frac{1}{\sin \beta} - \tan \frac{\beta}{2} \right)$$

$$N_A = W_A \cos \beta$$

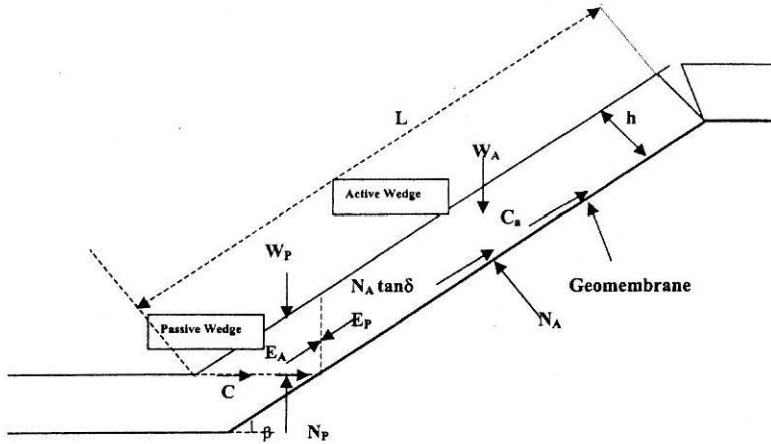


FIGURE 4 : Limit Equilibrium Forces involved in a Finite Length Slope Analysis for a Uniformly Thick Cover Soil

$$C_a = c_a \left[ \frac{(L-h)}{\sin \beta} \right]$$

$$W_p = \frac{\gamma h^2}{\sin 2\beta}$$

$$N_p = W_p + E_p \sin \beta$$

$$C = \frac{ch}{\sin \beta}$$

where

$W_A$  = total weight of the active wedge

$W_p$  = total weight of the passive wedge

$\gamma$  = Unit weight of the cover soil

$N_A$  = effective force normal to the failure plane of the active wedge

$\beta$  = Soil slope angle beneath the geomembrane

$\phi$  = Friction angle of the cover soil

$\delta$  = interface friction angle between cover soil and geomembrane

$h$  = uniform thickness of the cover soil

$L$  = length of slope measured along the geomembrane

$C_a$  = adhesive force between cover soil of the active wedge and geomembrane

$c_a$  = adhesion between cover soil of the active wedge and geomembrane

$C$  = cohesive force along the failure plane of the passive wedge

$c$  = cohesion of the cover soil

$E_A$  = inter-wedge force acting on the active wedge from the passive wedge and

$E_p$  = inter-wedge force acting on the passive wedge from the active wedge

$$E_A = \frac{(FS)(W_A - N_A \cos \beta) - (N_A \tan \delta + C_a) \sin \beta}{\sin \beta (FS)}$$

$$E_p = \frac{C + W_p \tan \phi}{\cos \beta (FS) - \sin \beta \tan \phi}$$

On equating  $E_A$  and  $E_p$  a quadratic equation is formed from which FS is obtained as under

$$FS = \frac{(-b + \sqrt{b^2 - 4ac})}{2a} \quad (1)$$

where

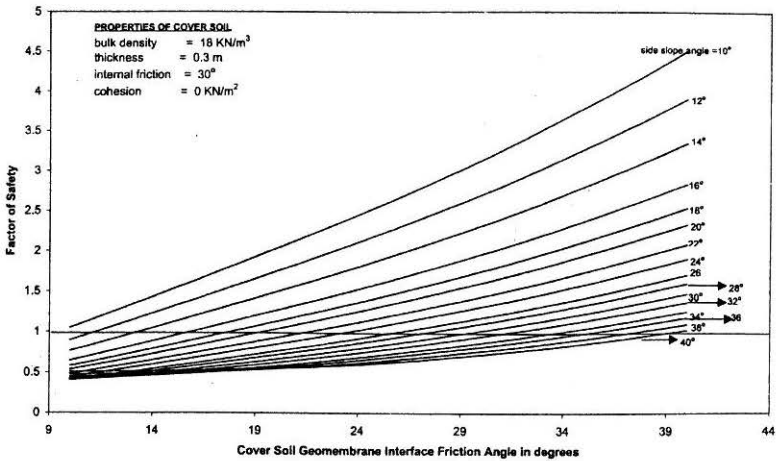
$$a = (W_A - N_A \cos \beta) \cos \beta$$

$$b = - \left[ \begin{array}{l} (W_A - N_A \cos \beta) \sin \beta \tan \phi \\ + (N_A \tan \delta + C_a) \sin \beta \cos \beta \\ + \sin \beta (C + W_p \tan \phi) \end{array} \right]$$

$$c = (N_A \tan \beta + C_a) \sin^2 \beta \tan \phi$$

A FS value greater than 1.0 must be targeted. In the above analysis situations like seepage forces, seismic forces and construction equipment have not been considered.

A program was developed to obtain FS-values for typical soil



**FIGURE 5 : Design Chart, Factor of Safety for Cover Soil Slope Stability (Gravitational Forces only)**

characteristics for various slope angles  $\beta$  and interface friction angle  $\delta$ . The results are given as design chart as per Fig.5.

### *Gravitational Forces of Cover Soil and Construction Equipment on Slope*

Earth moving equipment weighing  $W_b$  is used to place the cover soil on the liner material. It is desirable to place the cover soil from toe upward to the crest. This is because the gravitational forces of the cover soil and live load of the construction equipment are compacting previously placed soil and working with an ever-present passive wedge and stable lower portion beneath the active wedge. The reduction of FS value due to equipment on slope moving upward is relatively small compared to the equipment moving downward. The earth moving equipment and the equipment forces are shown in Figs.(6a) to (6d).

In the first case when the equipment moves up slope: the term ' $W_e$ ' is added to ' $W_A$ ' and the analysis is carried like that of gravitational forces. Fig.6c is used for the analysis as given in Poulos and Davis (1974).

In case of equipment moving down: slope is inevitable then a dynamic force per unit width at the cover soil to geomembrane interface, ' $F_e$ ', is taken into account as shown in Fig.(6d).



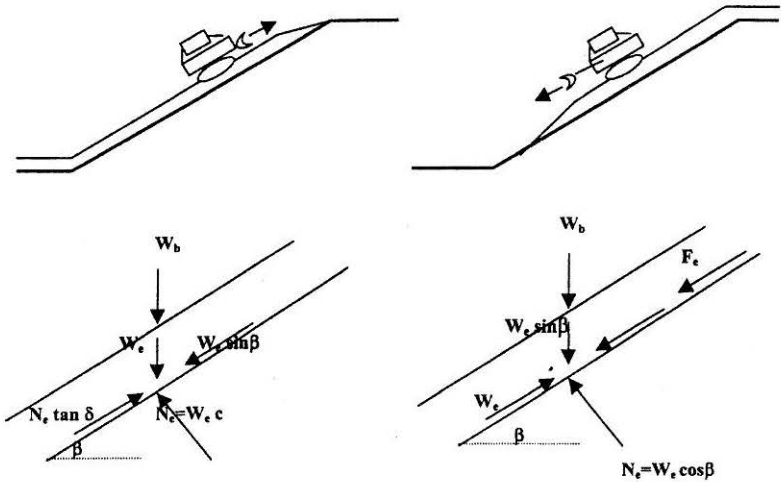


FIGURE 6 : (a) Equipment Back-filling Up Slope; (b) Equipment Back-filling Down Slope; (c) Equipment Moving Up Slope; (d) Equipment Moving Down Slope

$$E_A = \frac{(FS)[(W_A + W_e) \sin \beta + F_e]}{FS} - \frac{[(N_e + N_A) \tan \delta + C_a]}{FS}$$

$$E_p = \frac{(C + W_p \tan \phi)}{[\cos \beta (FS) - \sin \beta \tan \phi]}$$

where

$W_b$  = weight of the equipment

$W_e$  = equivalent equipment force per unit width at the Geomembrane interface =  $qwl$

$q = W_b(2wb)$ , where  $b$  = width of track and  $w$  = length of track

$I$  = influence factor at the geomembrane interface

$N_e$  = effective equipment force normal to the failure plane of the active wedge

$F_e$  = dynamic force per unit width parallel to the slope at the geomembrane interface

=  $W_e(a/g)$ , where  $a$  = acceleration of the equipment and  $g$  = acceleration due to gravity

Poulos and Davis (1974) gave values of 'I' and 'a'. Here the forces  $E_A$  and  $E_p$  are equated to find out the factor of safety. On equating,

$$a = [(W_A - W_e) \sin \beta + F_e] \cos \beta$$

$$b = - \left\{ \begin{array}{l} [(N_A + N_A) \tan \delta] \\ + [(W_A + W_e) \sin \beta + F_e] \sin \beta \tan \varphi + (C + W_p \tan \varphi) \end{array} \right\}$$

$$c = [(N_e + N_A) \tan \delta + C_a] \sin \beta \tan \phi$$

The factor of safety is calculated using Eqn. (1).

In this case of construction equipment on slope a program was developed to obtain FS-values for typical soil characteristics for various slope angles  $\beta$  and interface friction angle  $\delta$ . The results are given as design chart as per Fig.7.

### Gravitational Forces of Cover Soil and Seepage Forces

If adequate drainage facility of the cover soil then seepage-induced slope stability problems will occur. This seepage builds up in two different ways a horizontal buildup from the toe upward or a parallel-to-slope buildup outward along the slope. Here analysis is done again using the free-body diagram of active and passive wedges including the pore water pressures. Fig.8 shows the both the seepage conditions.

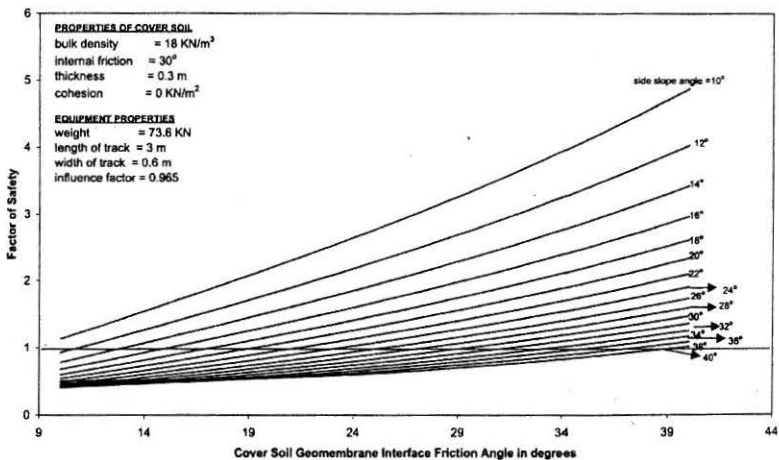


FIGURE 7 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Earth Moving Equipment on Slope

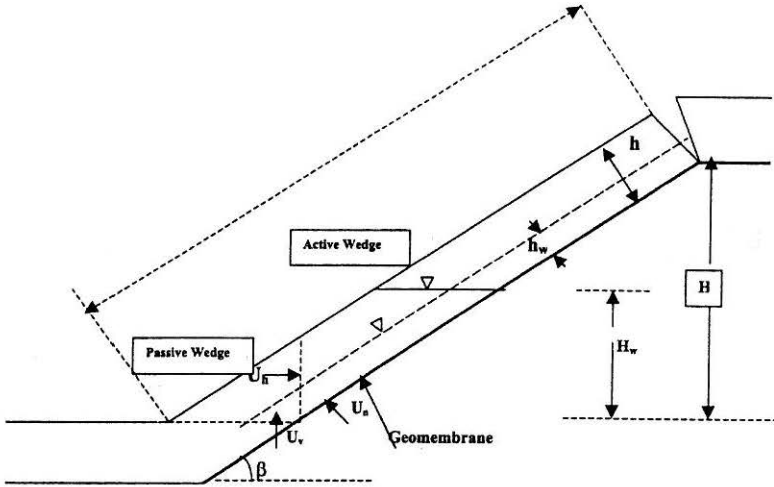


FIGURE 8 : Different Submergence Conditions for Seepage Forces Analysis

The situations which results in seepage induced slides are:

- Drainage soil with very low hydraulic conductivity
- Inadequate drainage capacity at the toe
- Clogging of drainage layer due to accumulation of fines at the toe of the slope
- Freezing of the drainage layer at the toe of the slope

Additional discussion on seepage induced slope failure is given by Soong and Koerner (1996).

### Horizontal seepage buildup

Horizontal seepage buildup can occur when toe blockage occurs due to inadequate outlet capacity, contamination or physical blocking of outlets, or freezing conditions at the outlets. The expressions due seepage condition are

$$W_A = \frac{\gamma_{\text{sat}} h (2H_w \cos \beta - h)}{\sin(2\beta)} + \frac{\gamma h (H - H_w)}{\sin \beta}$$

$$U_n = \frac{\gamma_w h \cos \beta (2H_w \cos \beta - h)}{\sin(2\beta)}$$

$$N_A = W_A \cos \beta + U_h \sin \beta - U_n$$

$$U_h = \gamma_w h^2 / 2$$

$$U_v = U_h \cot \beta$$

- where
- $U_h$  = resultant of the pore pressures acting on the inter-wedge surfaces
  - $U_n$  = resultant of the pore pressures acting perpendicular to the slope
  - $U_v$  = resultant of the vertical pore pressures acting on the passive wedge
  - $H$  = height of the landfill
  - $H_w$  = vertical height of the slope measured from the toe
  - $h_w$  = height of free water surface measured in the direction perpendicular to the slope
  - $\gamma_{sat}$  = saturated unit weight of cover soil

The values of  $a$ ,  $b$  and  $c$  to be used for calculation of FS are given in Parallel-to-slope seepage build up and the same is also applicable for horizontal seepage buildup.

### Parallel-to-slope seepage build-up

Parallel seepage build-up can occur when soils placed above a geomembrane are initially too low in their hydraulic conductivity, or become too low due to long-term clogging from overlying soils, which do not have a filter. The expressions are,

$$W_A = \frac{\gamma(h-h_w)[2H\cos\beta-(h+h_w)]}{\sin(2\beta)} + \frac{\gamma_{sat}h_w(2H\cos\beta-h_w)}{\sin(2\beta)}$$

$$U_n = \frac{\gamma_w h_w \cos\beta(2H\cos\beta-h_w)}{\sin(2\beta)}$$

$$U_h = \frac{\gamma_w (h_w)^2}{2}$$

$$W_p = \frac{[\gamma(h^2-h_w^2) + \gamma_{sat}(h_w)^2]}{\sin(2\beta)}$$

After obtaining the expressions the forces  $E_A$  and  $E_p$  are also obtained and equated to get the values for  $a$ ,  $b$  and  $c$  as;

$$a = W_A \sin \beta \cos \beta - U_h \cos^2 \beta + U_h$$

$$b = -W_A \sin^2 \beta \tan \phi - U_h \sin \beta \cos \beta \tan \phi \\ - N_A \cos \beta \tan \delta - (W_p - U_v) \tan \phi$$

$$c = N_A \sin \beta \tan \delta \tan \phi$$

As with previous solutions, the resulting FS value is obtained using Eqn (1).

In this case of seepage forces a program was developed to obtain FS-values for typical soil characteristics for various slope angles  $\beta$  and interface friction angle  $\delta$ . The results are given as design charts as per Figs.9 and 10.

### Gravitational Forces of Cover Soil and Seismic Forces

In areas with anticipated earthquake activity, the slope stability analysis of a cover soil must consider seismic forces. The analysis is a two-part process.

- The calculation of a FS value using a pseudo-static analysis by adding a horizontal force (seismic) acting at the centroid of the cover soil cross section.

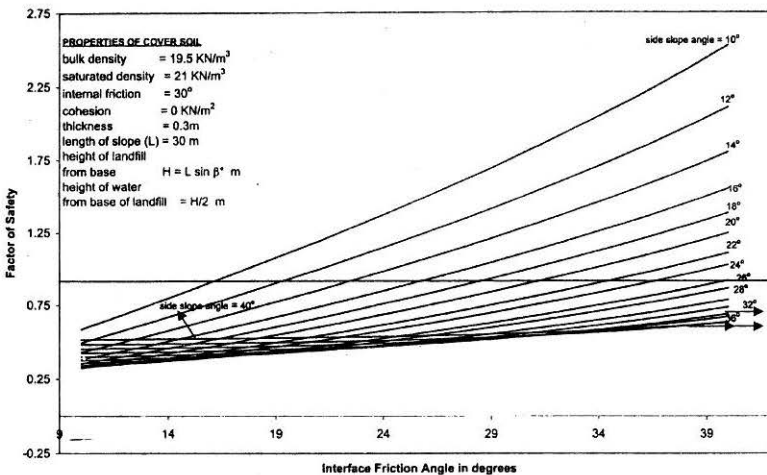
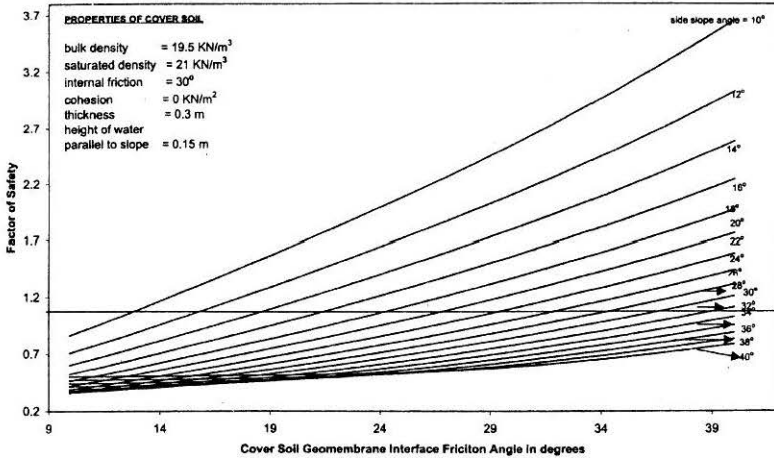


FIGURE 9 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Horizontal Seepage Forces



**FIGURE 10 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Seepage Forces Parallel to the Slope**

- A permanent deformation analysis if the FS value calculated as above is less than 1.0.

In the first part: only a horizontal force at the centroid of the cover soil in proportion to the anticipated seismic activity is added. An average seismic coefficient ( $C_s$ ) is obtained. The value  $C_s$  is a non-dimensional ratio of the bedrock acceleration to gravitational acceleration. The bedrock acceleration can be estimated from a seismic zone map as given by Algermissen (1991). The free body diagram for analysis of seismic effect is shown in Fig.11.

Only the value of  $C_s$  is multiplied with ' $W_A$ ' and ' $W_p$ ' and added to ' $W_A$ ' and ' $W_p$ ' respectively and the rest of the calculations are same as that of gravitational forces of the cover soil.

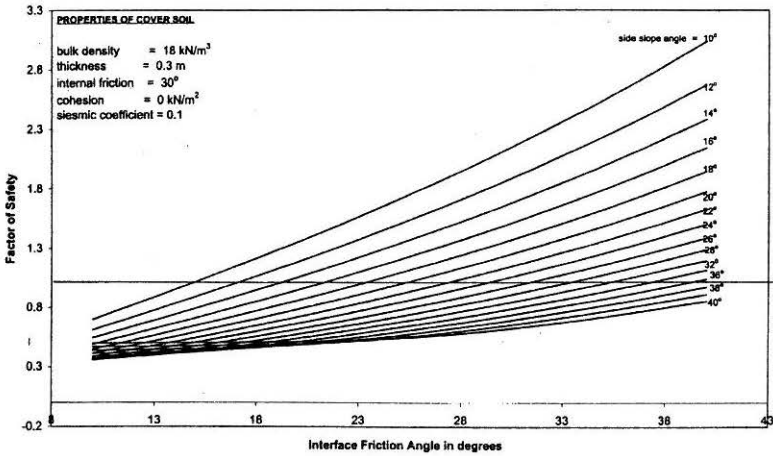
where

$C_s$  = average seismic coefficient

$$E_A = \frac{(FS)(C_s W_A + N_A \sin \beta)}{(FS)\cos \beta} - \frac{(N_A \tan \delta + C_a)}{(FS)\cos \beta}$$

$$E_p = \frac{C + W_p \tan \phi - C_s W_p (FS)}{[(FS)\cos \beta - \sin \beta \tan \phi]}$$





**FIGURE 12 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Seismic Forces**

of landfill for all conditions analyzed as above and keeping all the values as variables. By taking a typical example of soil parameter values the results are obtained as design charts for varying slope angles ( $\beta$ ) and interface friction angle ( $\delta$ ). The design charts are given along with each analysis. From the charts it can be understood that as the interface friction angle increases the FS increases and as the slope angle reduces the FS increases.

### **Situations Causing Enhanced Stabilization of Slopes**

The following are the situations, which can be adopted to enhance the stabilization of the slopes:

- Slopes with tapered thickness cover soil
- Reinforcement of the cover soil with geogrid or high strength geotextile

#### ***Slopes with Tapered Thickness Cover Soil***

The factor of safety can be considerably increased for a given slope by uniformly tapering the cover soil thickness from thick toe to thin crest (see Fig.13). The slope inclination ' $\beta$ ' is greater than the finished slope angle of the cover soil ' $\omega$ '. The earth pressure forces on the respective wedges oriented at the average of the slope and the cover soil angles.

$h_c$  = thickness of cover soil at crest of the slope

$w$  = finished slope angle of cover soil



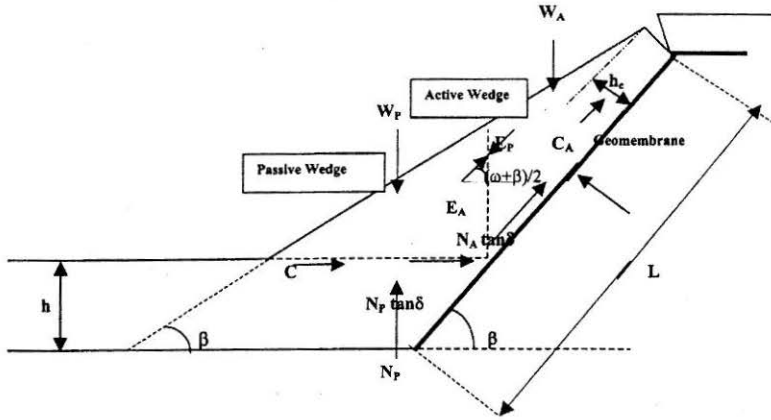


FIGURE 13 : Free Body Diagram for Analysis of Slope Stability with Tapered Cover Soil Thickness

$$y = \left( L - \frac{h}{\sin \beta} - h_c \tan \beta \right) (\sin \beta - \cos \beta \tan \omega)$$

$$N_A = W_A \cos \beta$$

$$W_A = \gamma \left[ \left( L - \frac{h}{\sin \beta} - h_c \tan \beta \right) \left( \frac{y \cos \beta}{2} + h_c \right) + \frac{h_c^2 \tan \beta}{2} \right]$$

$$C_a = c_a \left( L - \frac{h}{\sin \beta} \right)$$

$$W_p = \frac{\gamma}{2 \tan \omega} \left[ \left( L - \frac{h}{\sin \beta} - h_c \tan \beta \right) (\sin \beta - \cos \beta \tan \omega) + \frac{h_c}{\cos \beta} \right]^2$$

$$N_p = W_p + E_p \sin \left( \frac{\omega + \beta}{2} \right)$$

$$C = \frac{\gamma}{\tan \omega} \left[ \left( L - \frac{h}{\sin \beta} - h_c \tan \beta \right) (\sin \beta - \cos \beta \tan \omega) + \frac{h_c}{\cos \beta} \right]$$

After  $E_A$  and  $E_p$  are equated to get the values for a, b and c as;

$$a = (W_A - N_A \cos \beta) \cos \left( \frac{\omega + \beta}{2} \right)$$

$$b = \left[ \begin{aligned} & \left\{ (W_A - N_A \cos \beta) \sin \left( \frac{\omega + \beta}{2} \right) \tan \phi \right\} \\ & + \left\{ (N_A \tan \delta + C_a) \sin \beta \cos \left( \frac{\omega + \beta}{2} \right) \right\} \\ & + \left\{ \sin \left( \frac{\omega + \beta}{2} \right) (C + W_p \tan \phi) \right\} \end{aligned} \right]$$

$$c = (N_A \tan \delta + C_a) \sin \beta \sin \left( \frac{\omega + \beta}{2} \right) \tan \phi$$

As with previous solution, the resulting FS value is obtained using Eqn.(1).

A program was developed to obtain FS-values for typical soil characteristics for various slope angles  $\beta$  and finished slope angle  $\omega$ . The results are given as design chart as per Fig.14.

### Reinforcement of the Cover soil

Another way of increasing a given slope's factor of safety is to

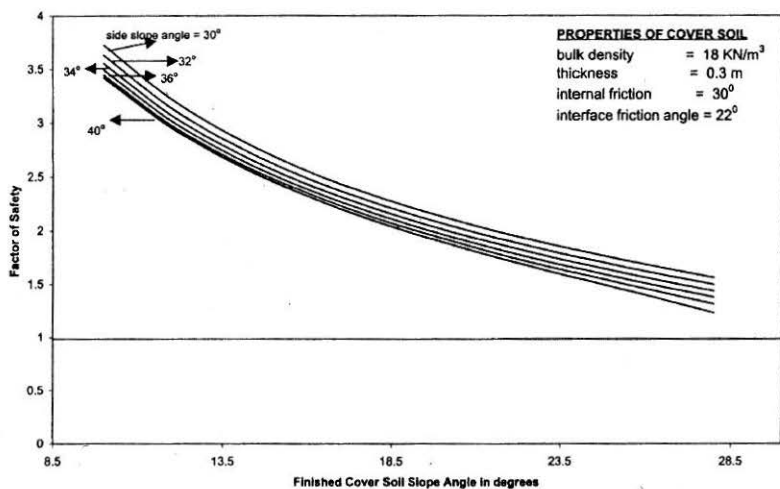


FIGURE 14 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Tapered Thickness

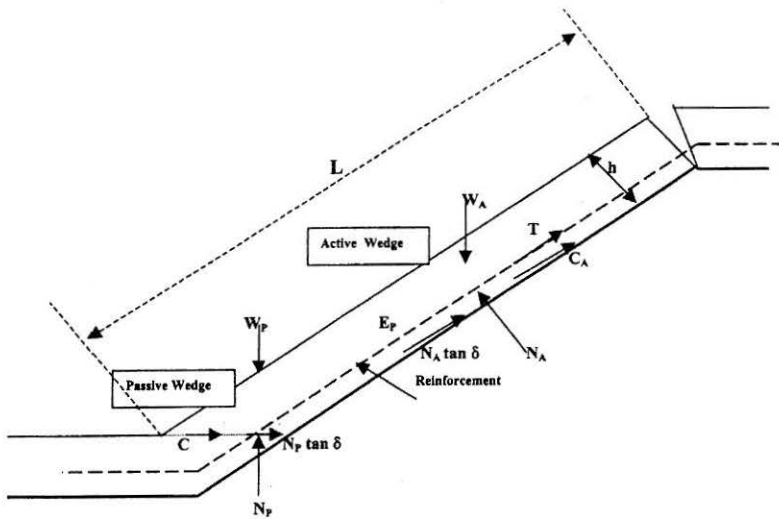


FIGURE 15 : Free Body Diagram for Slope Analysis with Reinforcement of Cover Soil

reinforce it with a geosynthetic material. Fig.15 shows the reinforcement force 'T'.

Here the term 'T' is the allowable strength of the geosynthetics reinforcement inclusion. The allowable 'T' is obtained by applying reduction factors as shown below.

$$T \text{ (allowable)} = \frac{T \text{ (ultimate)}}{(RF1 * RF2 * RF3*)}$$

RF1 = reduction factor for installation damages

RF2 = reduction factor for creep

RF3 = reduction factor for long term chemical /biological degradation

This force 'T' will enhance the resisting forces.

As usual the forces  $E_A$  and  $E_P$  are obtained and equated to get the values for a, b and c as;

$$a = (W_A - N_A \cos \beta - T \sin \beta) \cos \beta$$

$$b = - \left[ \begin{array}{l} (W_A - N_A \cos \beta - T \sin \beta) \sin \beta \tan \phi \\ + (N_A \tan \delta + C_a) \sin \beta \cos \beta + \sin \beta (C + W_p \tan \phi) \end{array} \right]$$

$$c = (N_A \tan \delta + C_a) \sin^2 \beta \tan \phi$$

Again, the resulting FS value can be obtained using Eqn.(1).

### Program and Results

A program is made to estimate the factor of safety for the above mentioned two conditions. As an example, typical soil characteristics were chosen to run the program and the results are shown in Figs.14 and 16. It can be observed that in the charts the reinforcement provided does not substantially increase the FS value whereas the tapered thickness, even with 2 degrees of difference from top and bottom has improved the FS value substantially.

## Design of Thickness and Anchorage of Geomembrane Liner

### Thickness of the Geomembrane

Koerner (1998) proposed the thickness considerations for the geomembrane for landfills and liquid containment. The basic model along

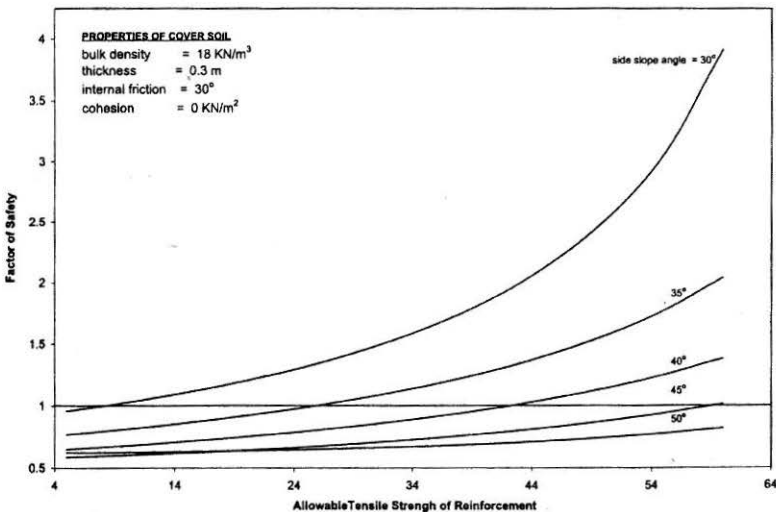


FIGURE 16 : Design Chart, Factor of Safety for Cover Soil Slope Stability with Geosynthetic Reinforcement

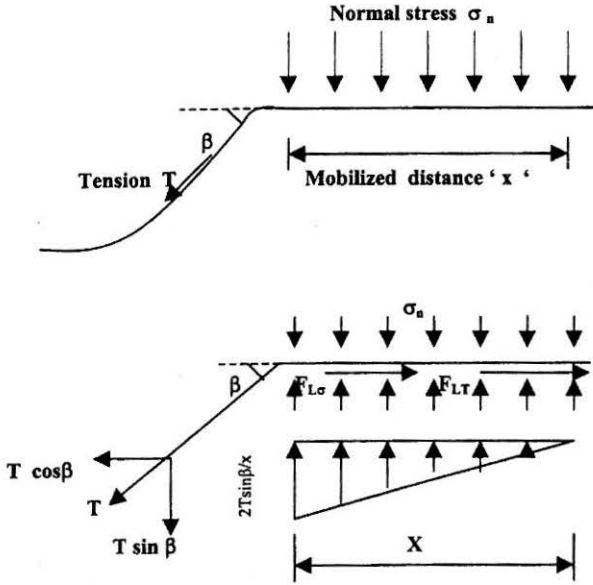


FIGURE 17 : Design Model and Related Forces used to Calculate Geomembrane Thickness

with the forces adopted by him was based on deformation-mobilised tensile force as shown in the Fig.17. The basic relationship is given by

$$T = \sigma_{\text{allow}} t$$

where  $T$  = tension mobilised in the geomembrane  
 $\sigma_{\text{allow}}$  = allowable geomembrane stress, and  
 $t$  = thickness of the geomembrane

After resolving the forces in the horizontal direction and taking  $\sum F_x = 0$  we get

$$T \cos \beta = \sigma_n \tan \delta_u(x) + \sigma_n \tan \delta_L(x) + 0.5 \left( 2T \frac{\sin \beta}{x} \right) (x) \tan \delta_L$$

$$T = \frac{\sigma_n x (\tan \delta_U + \tan \delta_L)}{\cos \beta - \sin \beta \tan \delta_L}$$

$$\text{Therefore thickness 't' } = \frac{\sigma_n x (\tan \delta_U + \tan \delta_L)}{\sigma_{\text{allow}} (\cos \beta - \sin \beta \tan \delta_L)}$$

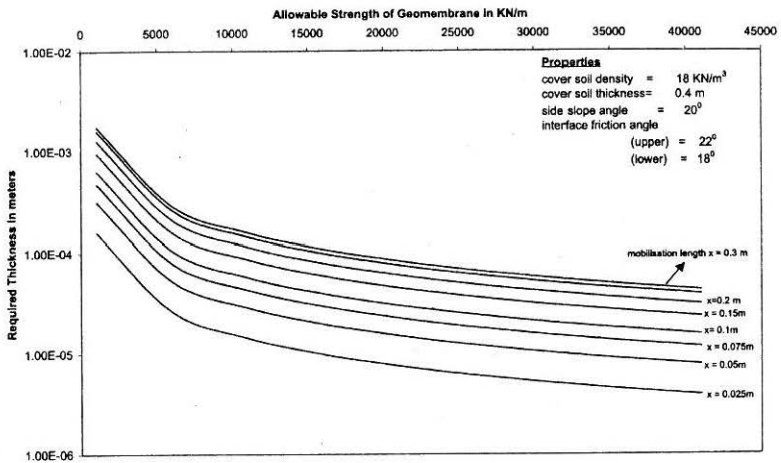


FIGURE 18 : Required Geomembrane Thickness for Various Slope Angles and Interface Angles

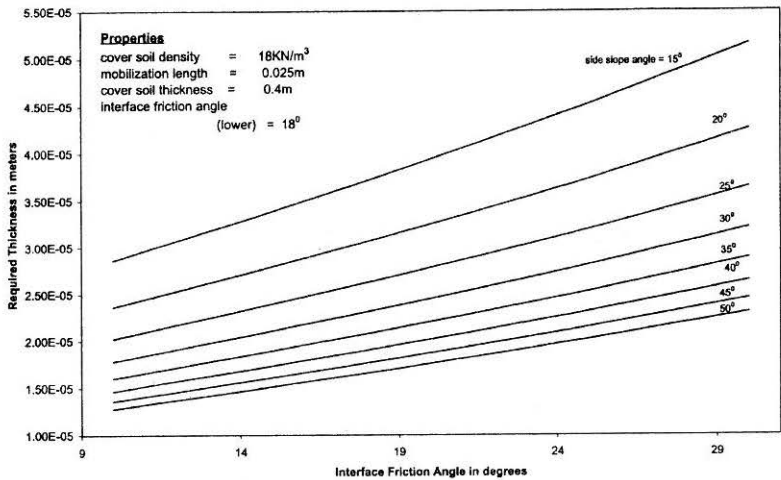


FIGURE 19 : Required Geomembrane Thickness for Various Allowable Strength and Mobilization Distances

where

$\beta$  = Settlement angle mobilising the geomembrane tension (side slope angle),

$\sigma_n$  = applied stress from the over lying cover soil,

$x$  = distance of mobilised geomembrane deformation,

$\delta_L$  = interface friction angle between geomembrane and the subgrade, and

$\delta_U$  = interface friction angle between geomembrane and the cover soil.

Based on the derived equation a computer program was written and results were obtained for the required thickness of the geomembrane for the landfill for various side slope angles and interface friction angle. Also a similar program was run to obtain the required thickness of the geomembrane for various allowable strength of the geomembrane and mobilised distance 'x'. The results obtained for typical cover soil characteristics are shown in Figs.18 and 19.

### Runout and Anchor Trench Design

For sufficient anchorage and holding of the geomembrane from slipping, the geomembrane should be extended to a distance (called the runout) away from the end of the slope or it should be taken vertically down into an anchor trench. Koerner (1998) analysed both cases i.e. runout and anchor trench considerations and obtained minimum runout length and depth required. The analysis as given below is based on the Fig.20.

From Fig.20 the horizontal force summation results, leads to the appropriate design equation.

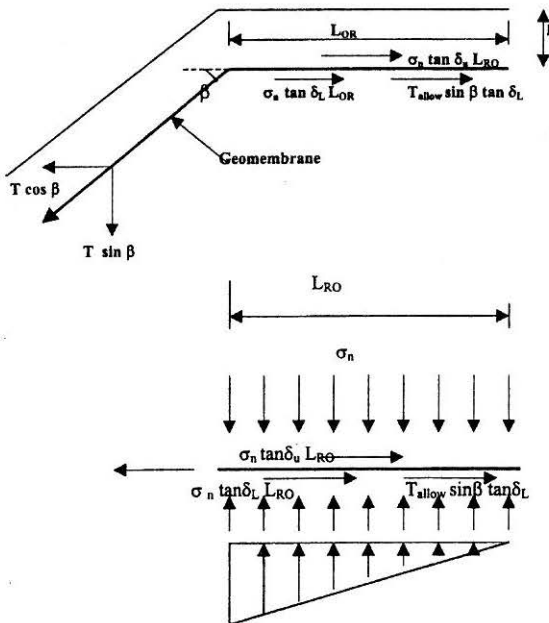


FIGURE 20 : Cross Section of Geomembrane Runout and Related Forces and Stresses

$$\sum F_x = 0$$

$$T_{\text{allow}} \cos \beta = \sigma_n \tan \delta_U (L_{\text{RO}}) + \sigma_n \tan \delta_L (L_{\text{RO}}) \\ + 0.5 \left( 2 T_{\text{allow}} \frac{\sin \beta}{L_{\text{RO}}} \right) (L_{\text{RO}}) \tan \delta_L$$

$$L_{\text{RO}} = \frac{T_{\text{allow}} (\cos \beta - \sin \beta \tan \delta_L)}{\sigma_n x (\tan \delta_U + \tan \delta_L)}$$

where

$L_{\text{RO}}$  = minimum required length of the geomembrane runout

$T_{\text{allow}}$  = allowable force in the geomembrane i.e.  $\sigma_{\text{allow}} t$

$\sigma_{\text{allow}}$  = allowable stress in the geomembrane, and

$t$  = thickness of the geomembrane

$\beta$  = Settlement angle mobilising the geomembrane tension (side slope angle)

$\sigma_n$  = applied stress from the over lying cover soil

$x$  = distance of mobilised geomembrane deformation

$\delta_L$  = interface friction angle between geomembrane and the subgrade

$\delta_U$  = interface friction angle between geomembrane and the cover soil

$h$  = cover soil thickness

The situation for anchor trench depth is shown in Fig.21. An active earth pressure ( $P_A$ ) is tending to destabilize the situation, whereas a passive earth pressure ( $P_p$ ) is tending to resist pullout.

Using the free body diagram forces  $\sum F_x = 0$

$$T_{\text{allow}} \cos \beta = \sigma_n \tan \delta_U (L_{\text{RO}}) + \sigma_n \tan \delta_L (L_{\text{RO}}) \\ + T_{\text{allow}} \sin \beta \tan \delta_L - P_A + P_p$$

$$P_A = 0.5(\gamma_{\text{AT}} d_{\text{AT}} + \sigma_n) K_{\text{AT}} d_{\text{AT}}$$

$$P_p = 0.5(\gamma_{\text{AT}} d_{\text{AT}} + \sigma_n) K_p d_{\text{AT}}$$

Thus an equation with two unknown is obtained. So either the runout is fixed and required depth is obtained or vice-versa.



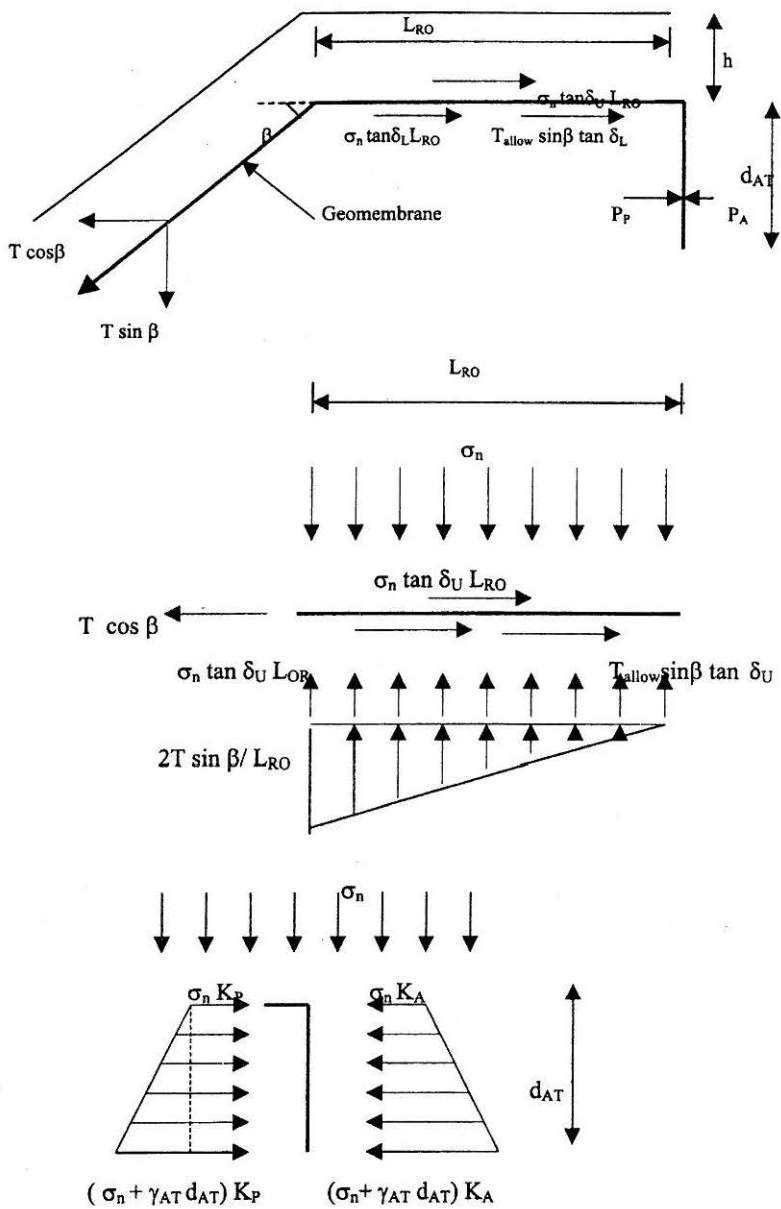


FIGURE 21 : Cross Section of Geomembrane Runout and Anchor Trench with Stress and Forces

- where
- LRO = minimum required length of the geomembrane runoff
  - $T_{\text{allow}}$  = allowable force in the geomembrane i.e.  $\sigma_{\text{allow}} t$
  - $\sigma_{\text{allow}}$  = allowable stress in the geomembrane, and
    - $t$  = thickness of the geomembrane
    - $\beta$  = settlement angle mobilising the geomembrane tension (side slope angle)
  - $\sigma_n$  = applied stress from the over lying cover soil
  - $x$  = distance of mobilised geomembrane deformation
  - $\delta_L$  = interface friction angle between geomembrane and the subgrade
  - $\delta_U$  = interface friction angle between geomembrane and the cover soil.
  - $\gamma_{\text{AT}}$  = unit weight of soil in anchor trench
  - $d_{\text{AT}}$  = depth of the anchor trench
  - $K_A$  = coefficient of active earth pressure =  $\tan^2(45 - \phi/2)$
  - $K_p$  = coefficient of passive earth pressure =  $\tan^2(45 + \phi/2)$
  - $P_A$  = active earth pressure against the backfill side of the anchor trench
  - $P_p$  = passive earth pressure against the backfill side of the anchor trench.

Based on the derived equation a computer program was written and results were obtained for the required runoff of the geomembrane for the landfill for various side slope angles and interface friction angle. Also a similar program was run to obtain the required runoff of the geomembrane for various allowable strength of the geomembrane and anchor trench depth. The results obtained for typical cover soil characteristics are shown in Figs.22 and 23.

## Summary

Here the slope stability of the cover soil on top of the geomembrane barrier liner was studied for various conditions and enhancements of the slope stability were also suggested. This analysis also can be applied to drainage soils placed on lined slopes beneath the waste. All the analysis are based on the concept of limit equilibrium with different assumptions involving particular details like

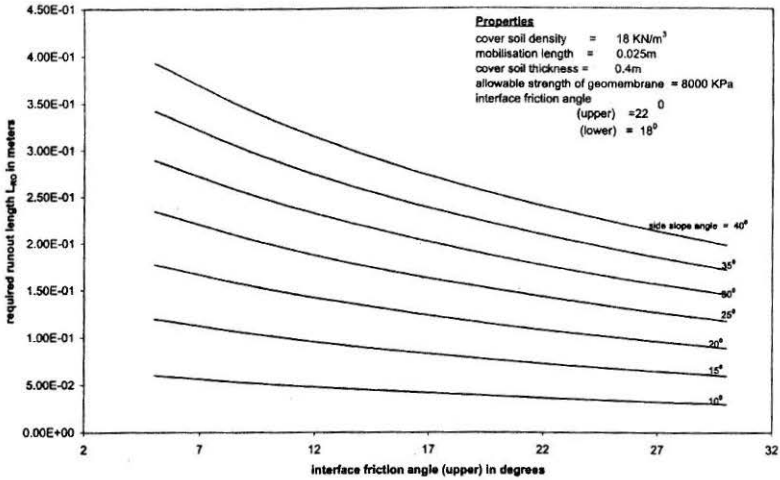


FIGURE 22 : Required Runout Length of Geomembrane for Landfill

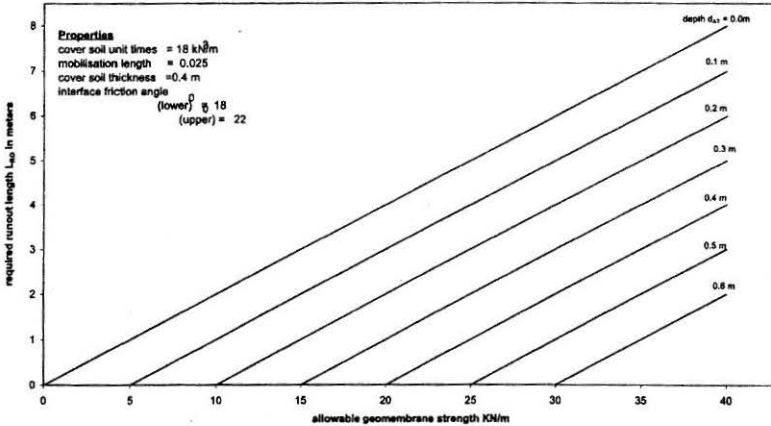


FIGURE 23 : Required Runout Length for Various Repts

- Existence of a tension crack at the top of slope (filled or unfilled)
- Orientation of the failure planes (linear) beneath the passive wedge
- Specific details of construction equipment movement on the slopes
- Specific details on seepage forces within the cover soil layer
- Specific details on seismic forces, particularly the magnitude and the selection of interface strengths

- Selection of strengths (allowable and ultimate) of the geomembrane for thickness design and anchor design
- Interface friction angle of geomembrane with subgrade and cover soil for thickness and anchor designs
- Soil characteristics for running all the programs

The design charts are made based on typical soil characteristics of the cover soil however the program presented can be used to obtain the FS value for any site condition and soil characteristics.

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